

Comparing Linear, Quadratic and Exponential Functions

For 1 – 3 determine if the table represents a linear, quadratic or exponential function. Write a model for each and give the domain and range.

1.

x	f(x)
0	5
1	8
2	11
3	14
4	17

↘ +3
↘ +3
↘ +3
↘ +3

Linear

$y = 3x + 5$
D: \mathbb{R} ; \mathbb{R}

2.

x	f(x)
0	7
1	6
2	7
3	10
4	15

-1 > 2
1 > 2
3 > 2
5 > 2

Quadratic

$y = (x - 1)^2 + 6$
D: \mathbb{R} ; \mathbb{R}

3.

x	y
0	1
1	2
2	4
3	8
4	16

↘ × 2
↘ × 2
↘ × 2
↘ × 2

Exponential

$y = 1(2)^x$
D: \mathbb{R}
R: $(0, \infty)$

4. Name the type of model that fits each data collection. Write a model for each.

a.

$(-2, \frac{1}{4}), (-1, \frac{1}{2}), (0, 1), (1, 2), (2, 4)$ Exponential $y = 1(2)^x$

b.

$(-2, -3), (-1, -1), (0, 1), (1, 3), (2, 5)$ Linear $y = 2x + 1$

c.

$(-2, 5), (-1, 2), (0, 1), (1, 2), (2, 5)$ Quadratic $y = (x - 0)^2 + 1$

5.

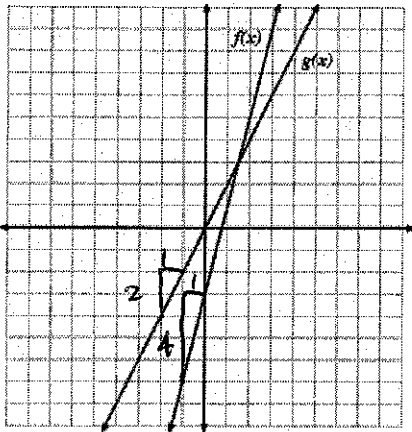
The change in the height of the ball from one bounce to the next if the ball is dropped from a height of 8 feet and the ball bounces to 80% of its previous height with each bounce.

$$8(.80)^x$$

Type of pattern of change .80 Exponential

How I found the pattern of change:

Take 80% of previous height bounce

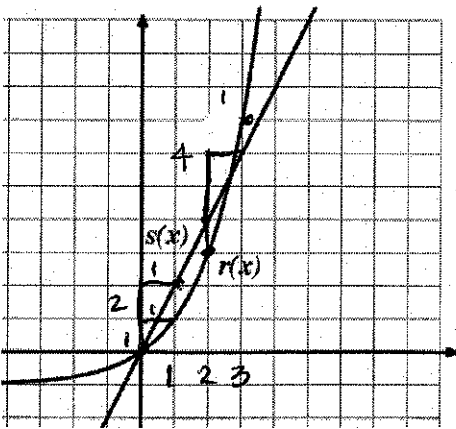


6. Which function has a greater rate of change? Explain.

$f(x)$

graph/line is steeper

$$f(x) = \frac{4}{1} > g(x) = \frac{2}{1}$$



7a. Examine the graph at the left from 0 to 1.

Which graph do you think is growing faster?

$$s(x) = \frac{2}{1} \quad r(x) = \frac{1}{1} \quad s(x) \text{ is growing faster}$$

b. Now look at the graph from 2 to 3.

Which graph is growing faster in this interval?

$$s(x) = \frac{2}{1} \quad r(x) = \frac{4}{1}$$

$r(x)$ is growing faster over this interval

8.

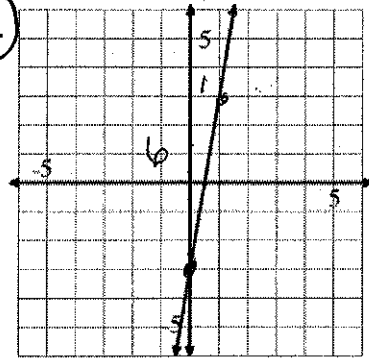
Identify whether situation "a" or situation "b" has the greater rate of change.

a.

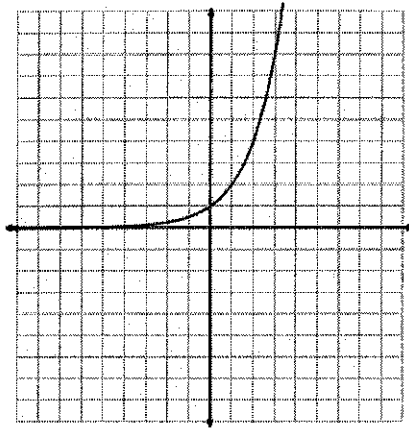
x	y
-10	-48
-9	-43
-8	-38
-7	-33

↘ 5
↘ 5
↘ 5

b.

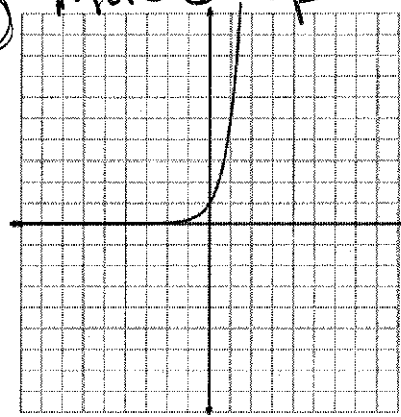


a.



b.

More Steep



a. Lee has \$25 withheld each week from his salary to pay for his subway pass.

$$25x$$

b.

Jose owes his brother \$50. He has promised to pay half of what he owes each week until the debt is paid.

$$\left(\frac{1}{2}\right)^x$$

* Exponentials always out beat linear functions *

a.

x	6	10	14	18
y	13	15	17	19

$+4$ $+4$ $+4$
 $+2$ $+2$ $+2$

$1/2$

a. $y = 2(5)^x$

larger rate

b. The number of rhombi in each shape.

Figure 1

Figure 2

Figure 3



$+2$

$+2$

b. In the children's book, *The Magic Pot*, every time you put one object into the pot, two of the same object come out. Imagine that you have 5 magic pots.

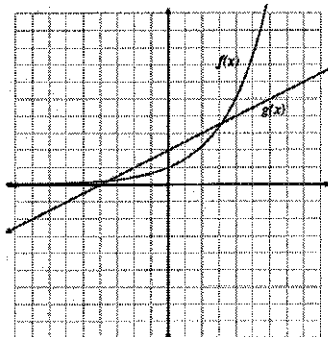
$5(2)^x$

9.

Compare the rates of change of each pair of functions by identifying the interval where it appears that $f(x)$ is changing faster and the interval where it appears that $g(x)$ is changing faster. Verify your conclusions by making a table of values for each equation and exploring the rates of change in your tables.

$f(x) = (1.5)^x$

$g(x) = \frac{1}{2}x + 2$



x	f(x)	g(x)
-2	0.4	1
-1	0.6	1.5
0	1	2
1	1.5	2.5
2	2.25	3
3	3.375	3.5

f
 $g(x)$ is greater $(-\infty, 3)$

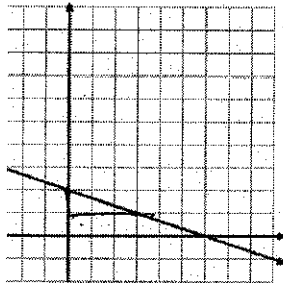
$f(x)$ is greater for x values greater than 3

11.

Write the explicit equation for the tables and graphs below.

x	f(x)
2	-4
3	-11
4	-18
5	-25

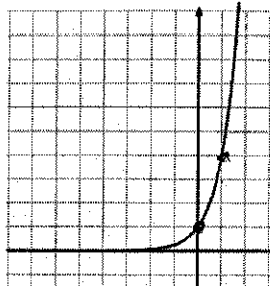
$-7x + 10$



$-3x + 2$

x	f(x)
-1	2/5
0	2
1	10
2	50

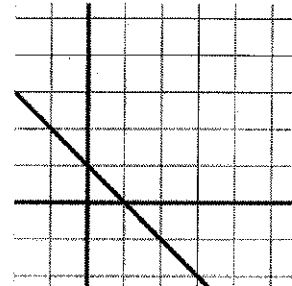
$2(5)^x$



$1(4)^x$

x	f(x)
2	-24
3	-48
4	-96
5	-192

$-6(2)^x$



$x + 1$

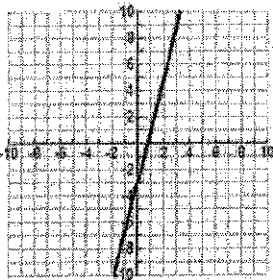
x	f(x)
-4	81
-3	27
-2	9
-1	3

$1(\frac{1}{3})^x$

12.

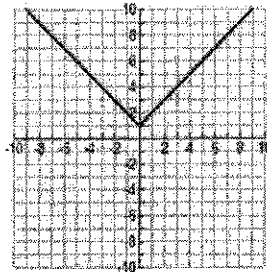
Determine whether the following functions are even, odd, or neither.

1. $f(x) = 4x^1 - 3x^0$



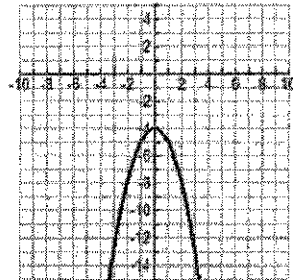
N

2. $f(x) = |x| + 1x^0$



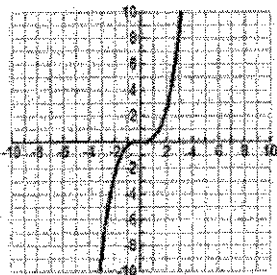
E

3. $f(x) = -x^2 - 4x^0$



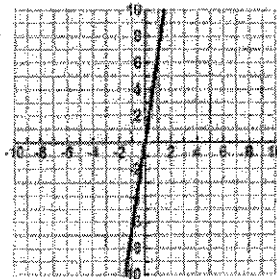
E

4. $f(x) = \frac{1}{3}x^3$



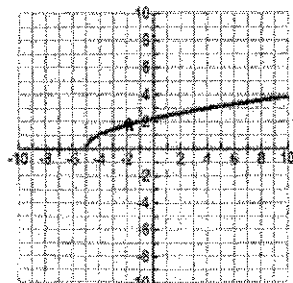
O

5. $f(x) = 7x^1$



O

6. $f(x) = \sqrt{x+5} \quad (x+5)^{1/2}$



N

$$7. f(x) = 3x^2$$

E

$$8. f(x) = x^3 - 2x^0$$

N

$$9. f(x) = 3x^1 + 4x^0$$

N

$$10. f(x) = x^2 - 5x^0$$

E

$$11. f(x) = 10x^1 + 5x^0$$

N

$$12. f(x) = 2(x+1)^3$$

~~E~~ N